# COMPUTATIONAL MATHEMATICS AND MATHEMATICAL PHYSICS

Cover-to-cover translation of
*Zhurnal vychislitel'noi matematiki i matematicheskoi fiziki*

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